Cladogenetic and Anagenetic Models of Chromosome Number Evolution: A Bayesian Model Averaging Approach

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Abstract — Chromosome number is a key feature of the higher-order organization of the genome, and changes in chromosome number play a fundamental role in evolution. Dysploid gains and losses in chromosome number, as well as polyploidization events, may drive reproductive isolation and lineage diversification. The recent development of probabilistic models of chromosome number evolution in the groundbreaking work by Mayrose et al. (2010), ChromEvol, has enabled the inference of ancestral chromosome numbers over molecular phylogenies and generated new interest in studying the role of chromosome changes in evolution. However, the ChromEvol approach assumes all changes occur anagenetically (along branches), and does not model events that are specifically cladogenetic. Cladogenetic changes may be expected if chromosome changes result in reproductive isolation. Here we present a new class of models of chromosome number evolution (called ChromoSSE) that incorporate both anagenetic and cladogenetic change. The ChromoSSE models allow us to determine the mode of chromosome number evolution; is chromosome evolution occurring primarily within lineages, primarily at lineage splitting, or in clade-specific combinations of both? Furthermore, we can estimate the location and timing of possible chromosome speciation events over the phylogeny. We implemented ChromoSSE in a Bayesian statistical framework, specifically in the software RevBayes, to accommodate uncertainty in parameter estimates while leveraging the full power of likelihood based methods. We tested ChromoSSE’s accuracy with simulations and re-examined chromosomal evolution in Aristolochia, Canes section Spinorchis, Helianthus, Mimulus sensu lato (s.l.), and Primula section Alcarieta, finding evidence for clade-specific combinations of anagenetic and cladogenetic dysploid and polyploid modes of chromosome evolution. [Anagenetic; Bayes factors; chromosome evolution; chromosome speciation; chromoSSE; cladogenetic; dysploidy; phylogenetic models; polyploidy; reversible-jump Markov chain Monte Carlo; whole genome duplication.]

A central organizing component of the higher-order architecture of the genome is chromosome number, and changes in chromosome number have long been understood to play a fundamental role in evolution. In the seminal work Genetics and the Origin of Species (1937), Dobzhansky identified “the raw materials for evolution,” the sources of natural variation, as two evolutionary processes: mutations and chromosome changes. “Chromosomal changes are one of the mainsprings of evolution,” Dobzhansky asserted, and changes in chromosome number such as the gain or loss of a single chromosome (dysploidy), or the doubling of the entire genome (polyploidy), can have phenotypic consequences, affect the rates of recombination, and increase reproductive isolation among lineages and thus drive diversification (Shelbourn 1971). Recently, evolutionary biologists have studied the macroevolutionary consequences of chromosome changes within a molecular phylogenetic framework, mostly due to the groundbreaking work of Mayrose et al. (2010, ChromEvol) which introduced likelihood-based models of chromosome number evolution. The ChromEvol models have permitted phylogenetic studies of ancient whole genome duplication events, rapid “catastrophic” chromosome speciation, major reevaluations of the evolution of angiosperms, and new insights into the fate of polyploid lineages (e.g., Pires and Hertweck 2008, Mayrose et al. 2011; Tank et al. 2015).

One aspect of chromosome evolution that has not been thoroughly studied in a probabilistic framework is cladogenetic change in chromosome number. Cladogenetic changes occur solely at speciation events, as opposed to anagenetic changes that occur within lineages and are not associated with speciation events. Studying cladogenetic chromosome changes in a phylogenetic framework has been difficult since the approach used by ChromEvol models only anagenetic changes and ignores the changes that occur specifically at speciation events and may be expected if chromosome changes result in reproductive isolation. Reproductive incompatibilities caused by chromosome changes may play an important role in the speciation process, and led White (1978) to propose that chromosome changes perform “the primary role in the majority of speciation events.” Indeed, chromosome fusions and fissions may have played a role in the formation of reproductive isolation and speciation in the great apes (Ayala and Coluzzi 2005), and the importance of polyploidization in plant speciation has long been appreciated (Coynie and Orr 2004; Rieseberg and Willis 2007). Recent work by Zhan et al. (2016) revealed phylogenetic evidence that polyploidization is frequently cladogenetic in land plants. However, their approach did not examine the role dysploid changes may play in speciation, and it required a two-step analysis in which one first used ChromEvol to infer ploidy levels, and then a second modeling step to infer the proportion of ploidy shifts.
that were cladogenetic. Since ChromEvol only models anagenetic polyploidization events these two modeling steps are inconsistent with one another.

Here we present models of chromosome number evolution that simultaneously account for both cladogenetic and anagenetic polyploidy as well as dysploid changes in chromosome number over a phylogeny. These models reconstruct an explicit history of cladogenetic and anagenetic changes in a clade, enabling estimation of ancestral chromosome numbers. Our approach also identifies different modes of chromosome number evolution among clades; we can detect primarily anagenetic, primarily cladogenetic, or clade-specific combinations of both modes of chromosome changes. Furthermore, these models allow us to infer the timing and location of possible polyploid and dysploid speciation events over the phylogeny. Since these models only account for changes in chromosome number, they ignore speciation that may accompany other types of chromosome rearrangements such as inversions. Our models cannot determine that changes in chromosome number “caused” the speciation event, but they do reveal that speciation and chromosome change are temporally correlated. Thus, these models can give us evidence that the chromosome number change coincided with cladogenesis and so may have played a significant role in the speciation process.

A major challenge for all phylogenetic models of cladogenetic character change is accounting for unobserved speciation events due to lineages going extinct and not leaving any extant descendants (Bokma 2002), or due to incomplete sampling of lineages in the present. Teasing apart the phylogenetic signal for cladogenetic and anagenetic processes given unobserved speciation events is a major difficulty. The Cladogenetic State change Speciation and Extinction (ClaSSE) model (Goldberg and Igi´c 2012) accounts for unobserved speciation events by jointly modeling both character evolution and the phylogenetic birth-death process. Our class of chromosome evolution models uses the ClaSSE approach, and could be considered a special case of ClaSSE. We implemented our models (called ChromoSSE) in a Bayesian framework and use Markov chain Monte Carlo algorithms to estimate posterior probabilities of the model’s parameters. However, compared with most character evolution models, SSE models require additional complexity since they must model extinction and speciation processes. Using simulations, we examined the impact of this additional complexity on our chromosome evolution models’ performance. Note that ChromoSSE uses the SSE approach to integrate over all unobserved speciation events and in this work we do not investigate how chromosome number affects diversification rates. Nonetheless, our implementation enables chromosome number dependent speciation and extinction rates to be estimated and this will be explored in future work.

Out of the class of ChromoSSE models described here, it is possible that no single model will adequately describe the chromosome evolution of a given clade. The most parameter-rich ChromoSSE model has at least 12 independent rate parameters, however the models that best describe a given data set (a phylogeny and a set of observed chromosome counts) may be special cases of the full model. For example, there may be a clade for which the best fitting models have no anagenetic rate of polyploidization (the rate \( \alpha = 0.0 \)) and for which all polyploidization events are cladogenetic. To explore the entire space of all possible models of chromosome number evolution we constructed a reversible jump Markov chain Monte Carlo (Green 1995) that samples across models of different dimensionality, drawing samples from chromosome evolution models in proportion to their posterior probability and enabling Bayes factors for each model to be calculated. This approach incorporates model uncertainty by permitting model-averaged inferences that do not condition on a single model; we draw estimates of ancestral chromosome numbers and rates of chromosome evolution from all possible models weighted by their posterior probability. For general reviews of this approach to model averaging (see Madigan and Raftery 1994; Kass and Raftery 1995; Hoeting et al. 1999), and for its use in phylogenetics (see Posada and Buckley 2004). Averaging over all models has been shown to provide a better average predictive ability than conditioning on a single model (Madigan and Raftery 1994). Conditioning on a single model ignores model uncertainty, which can lead to an underestimation in the uncertainty of inferences made from that model (Hoeting et al. 1999). In our case, this can lead to overconfidence in estimates of ancestral chromosome numbers and chromosome evolution parameter value estimates.

Our motivation in developing these phylogenetic models of chromosome evolution is to determine the mode of chromosome number evolution; is chromosome evolution occurring primarily within lineages, primarily at lineage splitting, or in clade-specific combinations of both? By identifying how much of the pattern of chromosome number evolution is explained by anagenetic versus cladogenetic change, and by identifying the timing and location of possible chromosome speciation events over the phylogeny, the ChromoSSE models can help uncover how much of a role chromosome changes play in speciation. In this paper, we first describe the ChromoSSE models of chromosome evolution and our Bayesian method of model selection, then we assess the models’ efficacy by testing them with simulated data sets, particularly focusing on the impact of unobserved speciation events on inferences, and finally we apply the models to five empirical data sets that have been previously examined using other models of chromosome number evolution.

METHODS
Models of Chromosome Evolution

In this section we introduce our class of probabilistic models of chromosome number evolution. We are interested in modeling the changes in chromosome
number both within lineages (anagenetic evolution) and at speciation events (cladogenetic evolution). The anagenetic component of the model is a continuous-time Markov process similar to Mayrose et al. (2010) as described below. The cladogenetic changes are accounted for by a birth-death process similar to Maddison et al. (2007) and Goldberg and Igic (2012), except each type of cladogenetic chromosome event is given its own rate. Thus, the birth-death process has multiple speciation rates (one for each type of cladogenetic change) and a constant single extinction rate. Our models of chromosome number evolution can therefore be understood as a specific case of the Cladogenetic State change Speciation and Extinction (ClaSSE) model (Goldberg and Igic 2012), which integrates over all possible unobserved speciation events (due to lineages that were unsampled or have gone extinct) directly in the likelihood calculation of the observed chromosome counts and tree shape. To test the importance of accounting for unobserved speciation events we also briefly describe a version of the model that handles different cladogenetic event types as transition probabilities at each observed speciation event and ignores unobserved speciation events, similar to the dispersal-extinction-cladogenesis (DEC) models of geographic range evolution (Ree and Smith 2008).

Our implementation assumes chromosome numbers can take the value of any positive integer, however to make likelihood calculations we follow Mayrose et al. (2010) in setting the maximum chromosome number \( C_{\text{m}} \) to \( n+10 \), where \( n \) is the highest chromosome number in the observed data. Note that we allow this parameter to be set in our implementation. Hence, it is easily possible to test the impact of setting a specific value for the maximum chromosome count.

Our models contain a set of six free parameters for anagenetic chromosome number evolution, a set of five free parameters for cladogenetic chromosome number evolution, an extinction rate parameter, and a vector of \( C_{\text{m},r} \) root frequencies of chromosome numbers, for a total of 12+\( C_{\text{m}} \) free parameters. All of the 11 chromosome rate parameters can be removed (fixed to 0.0) except the cladogenetic no-change rate parameter. Thus, the class of chromosome number evolution models described here has a total of \( 2^{11}=1024 \) nested models of chromosome evolution.

### Chromosome evolution within lineages

Chromosome number evolution within lineages (anagenetic change) is modeled as a continuous-time Markov process similar to Mayrose et al. (2010). The continuous-time Markov process is described by an instantaneous rate matrix \( Q \) where the value of each element represents the instantaneous rate of change within a lineage from a genome of \( i \) chromosomes to a genome of \( j \) chromosomes. For all elements of \( Q \) in which either \( i=0 \) or \( j=0 \) we define \( Q_{ij}=0 \). For the off-diagonal elements \( i \neq j \) with positive values of \( i \) and \( j \), \( Q \) is determined by:

\[
Q_{ij} = \begin{cases} 
\gamma_a e^{(j-i-1)/\lambda_a} & j = i+1, \\
\gamma_b e^{(j-i)/\lambda_b} & j = i-1, \\
\rho_a & j = 2i, \\
\nu_a & j = 1.5i, \\
0 & \text{otherwise},
\end{cases}
\]

where \( \gamma_a, \lambda_a, \rho_a, \) and \( \nu_a \) are the rates of chromosome gains, losses, polyploidizations, and demi-polyploidizations. \( \gamma_m \) and \( \beta_m \) are rate modifiers of chromosome gain and loss, respectively, that allow the rates of chromosome gain and loss to depend on the current number of chromosomes. This enables modeling scenarios in which the probability of fusion or fission events is positively or negatively correlated with the number of chromosomes. If the rate modifier \( \gamma_m=0 \), then \( \gamma_a e^{(j-i-1)/\lambda_a} = \gamma_a \). If the rate modifier \( \gamma_m > 0 \), then \( \gamma_a e^{(j-i-1)/\lambda_a} > \gamma_a \), and if \( \gamma_m < 0 \) then \( \gamma_a e^{(j-i-1)/\lambda_a} < \gamma_a \). These two rate modifiers replace the parameters \( \lambda_a \) and \( \nu_a \) in Mayrose et al. (2010), which in their parameterization may result in negative transition rates. Here we chose to exponentiate \( \gamma_m \) and \( \beta_m \) to ensure positive transition rates, and avoid ad hoc restrictions on negative transition rates that may induce unintended priors. Note that this assumes the rates of chromosome change can vary exponentially as a function of the current chromosome number, whereas Mayrose et al. (2010) assumes a linear function.

For odd values of \( i \), we set \( Q_{ij} = \eta_j/2 \) for the two integer values of \( j \) resulting when \( j = 1.5i \) was rounded up and down. We define the diagonal elements \( i = j \) of \( Q \) as:

\[
Q_{ii} = \sum_{j \neq i} C_{\text{m}} Q_{ij}.
\]

The probability of anagenetically transitioning from chromosome number \( i \) to \( j \) along a branch of length \( t \) is then calculated by exponentiation of the instantaneous rate matrix:

\[
P_{ij}(t) = e^{-Q_{ij}t}.
\]
all positive values of \( i, j, \) and \( k, \) we define:

\[
\lambda_{ijk} = \begin{cases} 
\phi_c & j = k = i \\
\gamma_c/2 & j = i + 1 \text{ and } k = i, \\
\gamma_c/2 & j = i \text{ and } k = i + 1, \\
\delta_c/2 & j = i - 1 \text{ and } k = i, \\
\delta_c/2 & j = i + 1 \text{ and } k = i, \\
\rho_c/2 & j = 2i \text{ and } k = i, \\
\rho_c/2 & j = i \text{ and } k = 2i, \\
\eta_c/2 & j = 1.5i \text{ and } k = i, \\
\eta_c/2 & j = i \text{ and } k = 1.5i, \\
0 & \text{otherwise}, 
\end{cases}
\]

(4)

so that the total speciation rate of the birth–death process \( \lambda_t \) is given by:

\[
\lambda_t = \phi_c + \gamma_c + \delta_c + \rho_c + \eta_c.
\]

(5)

Similar to the anagenetic instantaneous rate matrix described above, for odd values of \( i, \) we set \( \lambda_{ijk} = \eta_c/4 \) for the integer values of \( j \) and \( k \) resulting when \( 1.5i \) is rounded up and down. The extinction rate \( \mu \) is constant over the tree and for all chromosome numbers.

Note that this model allows only a single chromosome number change event on a maximum of one of the daughter lineages at each cladogenesis event. Changes in both daughter lineages at cladogenesis are not allowed; at least one of the daughter lineages must inherit the chromosome number of the ancestor. The model also assumes that cladogenesis events are always strictly bifurcating and that there are no hard polytomies.

**Likelihood calculation accounting for unobserved speciation.**—The likelihood of cladogenetic and anagenetic chromosome number evolution over a phylogeny is calculated using a set of ordinary differential equations similar to the Binary State Speciation and Extinction (BiSSE) model (Maddison et al. 2007). The BiSSE model was extended to incorporate cladogenetic changes by Goldberg and Igić (2012). Following Goldberg and Igić (2012), we define \( D_N(t) \) as the probability that a lineage with chromosome number \( i \) at time \( t \) evolves into the observed clade \( N. \) We let \( E_i(t) \) be the probability that a lineage with chromosome number \( i \) at time \( t \) goes extinct before the present, or is not sampled at the present. However, unlike the full ClaSSE model the extinction rate \( \mu \) does not depend on the chromosome number \( i \) of the lineage. The differential equations for these two probabilities is given by:

\[
\frac{dD_N(t)}{dt} = \left( \sum_{j=1}^{C_w} \sum_{k=1}^{C_w} \lambda_{ijk} + \sum_{j=1}^{C_w} Q_{ij} + \mu \right) D_N(t)
\]
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by an extinction event on one of the two daughter lineages. b) anagenetic change occurred, or a speciation event with a possible cladogenetic chromosome change occurred followed by extinction of both daughter lineages.

Figure 2. Chromosome evolution through time. An illustration of chromosome evolution events that could occur during each time interval \( \Delta t \) along the branches of a phylogeny. Equations 6 and 7 (a and b, respectively) sum over each possible chromosome evolution event and are numerically integrated backwards through time to the phylogeny to calculate the likelihood. a) \( D_N(t) \) is the probability that the lineage at time \( t \) evolves into the observed clade \( N \). To calculate the change in this probability over \( \Delta t \) we sum over three possibilities: no event occurred, an anagenetic change in chromosome number occurred, or a speciation event with a possible cladogenetic chromosome change occurred followed by an extinction event on one of the two daughter lineages. b) \( E_i(t) \) is the probability that the lineage goes extinct or is not sampled at the present. To calculate the change in this probability over \( \Delta t \) we sum over four possibilities: no event occurred followed eventually by extinction, extinction occurred, an anagenetic change occurred followed by extinction, or a speciation event with a possible cladogenetic change occurred followed by extinction of both daughter lineages.

\[
\frac{dD_N(t)}{dt} = \left( \sum_{j} \sum_{l} \lambda_{jk} + \sum_{j} Q_{jl} + \mu \right) D_N(t) + \sum_{j} Q_{ij} D_N(t) E_j(t) + D_{Nj}(t) E_j(t) E_k(t)
\]

\[
\frac{dE_i(t)}{dt} = \left( \sum_{j} \sum_{l} \lambda_{jk} + \sum_{j} Q_{jl} + \mu \right) E_j(t) + \mu + \sum_{j} Q_{ij} E_j(t)
\]

where again \( \lambda_{jk} \) for each possible cladogenetic event is given by equation 4. Letting \( D \) denote a set of observed chromosome counts, \( \Psi \) an observed phylogeny, and \( \theta \) a particular set of chromosome evolution model parameters, then the likelihood for the model parameters \( \theta \) is given by:

\[
P(D; \Psi; \theta) = \sum_{i=1}^{C_m} \prod_{j=1}^{C_m} \rho_{ij} D_{ij}(t),
\]

where \( \rho_{ij} \) is the root frequency of chromosome number \( i \) and \( D_{ij}(t) \) is the likelihood of the root node being in state \( i \) conditional on having given rise to the observed tree \( \Psi \) and the observed chromosome counts \( D \).

Initial conditions.—The initial conditions for each observed lineage at time \( t=0 \) for the extinction probabilities described by equation 7 are \( E_j(0) = 1 - \rho_j \) for all \( i \) where \( \rho_j \) is the sampling probability of including that lineage. For lineages with an observed chromosome number of \( i \), the initial condition is \( D_{Nj}(0) = \rho_i \). The initial condition for all other chromosome numbers \( j \) is \( D_{Nj}(0) = 0 \).

Likelihood calculation ignoring unobserved speciation.—To test the effect of unobserved speciation events on inferences of chromosome number evolution we
also implemented a version of the model described above that only accounts for observed speciation events. At each lineage divergence event over the phylogeny, the probabilities of cladogenetic chromosome number evolution \( P((i,k)|i) \) are given by the simplex \( \{ \phi_1, \phi_2, \phi_3, \phi_4, \phi_5 \} \), where \( \phi_1, \phi_2, \phi_3, \phi_4, \) and \( \phi_5 \) represent the probabilities of no change, chromosome gain, chromosome loss, polyploidization, and demiploidization, respectively. This approach does not require estimating speciation or extinction rates.

Here, we calculate the likelihood of chromosome number evolution over a phylogeny using Felsenstein’s pruning algorithm (Felsenstein 1981) modified to include cladogenetic probabilities similar to models of biogeographic range evolution (Landis et al. 2013; Landis 2017). Let \( D \) again denote a set of observed chromosome counts and \( \Psi \) represent an observed phylogeny where node \( l \) has descendant nodes \( m \) and \( n \). The likelihood of chromosome number evolution at node \( l \) conditional on node \( l \) being in state \( i \) and \( \theta_s \) being a particular set of chromosome evolution model parameter values is given by:

\[
P_l(D, \Psi| i, \theta_s) = \sum_{j=1}^{C_m} \sum_{k=1}^{C_m} P((j,k)|i) \left[ \sum_{m=1}^{C_m} \prod_{k=1}^{C_m} P_{ijk}(D_m|\Psi_m, \theta_{\Psi}) \right].
\]  

(10)

where the length of the branches between \( l \) and \( m \) is \( t_m \) and between \( l \) and \( j \) is \( t_j \). The state at the end of these branches near nodes \( m \) and \( n \) is \( j \) and \( k \), respectively. The state at the beginning of these branches, where they meet at node \( l \), is \( j \) and \( k \) respectively. The cladogenetic term sums over the probabilities \( P((j,k)|i) \) of all possible cladogenetic changes from state \( i \) to the states \( j \) and \( k \) at the beginning of each daughter lineage. The anagenetic term of the equation is the product of the probability of changes along the branches from state \( j \) to state \( k \) and state \( k \) to state \( k \) (given by equation 3) and the likelihood of the tree above node \( l \) recursively computed from the tips.

The likelihood for the model parameters \( \theta_s \) is given by:

\[
P(D, \Psi| \theta_s) = \sum_{i=1}^{C_m} \pi_i P_l(D, \Psi| i, \theta_s).
\]  

(11)

where \( P_l(D, \Psi| i, \theta_s) \) is the conditional likelihood of the root node being in state \( i \) and \( \pi_i \) is the root frequency of chromosome number \( i \).

Estimating parameter values and ancestral states.—For any given tree with a set of observed chromosome counts, there exists a posterior distribution of model parameter values and a set of probabilities for the ancestral chromosome numbers at each internal node of the tree.

Let \( P(\theta_s| D, \Psi) \) denote the joint posterior probability of \( \theta_s \) and a vector of specific ancestral chromosome numbers \( s_j \) given a set of observed chromosome counts \( D \) and an observed tree \( \Psi \). The posterior is given by Bayes’ rule:

\[
P(\theta_s, \Psi| D, \Psi) = \frac{P(D, \Psi| \theta_s, \Psi)}{\sum_{\theta_s} P(D, \Psi| \theta_s, \Psi)P(\theta_s|D, \Psi)}.
\]  

(12)

Here, \( P(\theta_s| D, \Psi) \) is the prior probability of the ancestral states \( s \) conditioned on the model parameters \( \theta_s \) and \( P(\theta_s| D, \Psi) \) is the joint prior probability of the model parameters.

In the denominator of equation 12 we integrate over all possible values of \( \theta \) and sum over all possible ancestral chromosome numbers \( s \). Since \( \theta \) is a vector of \( 12 + C_m \) parameters and \( s \) is a vector of \( n - 1 \) ancestral states where \( n \) is the number of observed tips in the phylogeny, the denominator of equation 12 requires a high-dimensional integral and an extremely large summation that is impossible to calculate analytically. Instead we use Markov chain Monte Carlo methods (Metropolis et al. 1953; Hastings 1970) to estimate the posterior probability distribution in a computationally efficient manner.

Ancestral states are inferred using a two-pass tree traversal procedure as described in Pupko et al. (2000), and previously implemented in a Bayesian framework by Huelsenbeck and Bollback (2001) and Pagel et al. (2004). First, partial likelihoods are calculated during the backwards-time post-order tree traversal in equations 6 and 7. Joint ancestral states are then sampled during a pre-order tree traversal in which the root state is first drawn from the marginal likelihoods at the root, and then states are drawn for each descendant node conditioned on the state at the parent node until the tips are reached. Again, we must numerically integrate over a system of differential equations during this root-to-tip tree traversal. This integration, however, is performed in forward-time, thus the set of ordinary differential equations must be slightly altered since our models of chromosome number evolution are not time reversible. Accordingly, we calculate:

\[
\frac{dD_{Nj}(t)}{dt} = -\left( \sum_{j=1}^{C_m} \sum_{k=1}^{C_m} k_{jk} + \sum_{j=1}^{C_m} Q_{ij} \right) D_{Nj}(t)
\]

\[
+ \sum_{j=1}^{C_m} Q_{ij} D_{Nj}(t)
\]

\[
+ \sum_{j=1}^{C_m} k_{jk} D_{Nj}(t)E_{jk}(t) + D_{Nk}(t)E_{jk}(t)
\]  

(13)
Table 1. Model parameter names and prior distributions

<table>
<thead>
<tr>
<th>Parameter</th>
<th>(X)</th>
<th>(f(X))</th>
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<tbody>
<tr>
<td>Cladogenetic</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Chromosome gain rate</td>
<td>(\gamma_g)</td>
<td>Exponential ((\Psi_1/2))</td>
</tr>
<tr>
<td>Chromosome loss rate</td>
<td>(\beta_g)</td>
<td>Exponential ((\Psi_1/2))</td>
</tr>
<tr>
<td>Polyploidization rate</td>
<td>(\nu_p)</td>
<td>Exponential ((\Psi_1/2))</td>
</tr>
<tr>
<td>Demi-polyploidization rate</td>
<td>(\eta_p)</td>
<td>Exponential ((\Psi_1/2))</td>
</tr>
<tr>
<td>Linear component of chromosome gain rate</td>
<td>(\gamma_m)</td>
<td>Uniform ((-3/C_m, 3/C_m))</td>
</tr>
<tr>
<td>Linear component of chromosome loss rate</td>
<td>(b_m)</td>
<td>Uniform ((-3/C_m, 3/C_m))</td>
</tr>
<tr>
<td>Other</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Root frequencies</td>
<td>(\pi)</td>
<td>Dirichlet ((1, \ldots, 1))</td>
</tr>
<tr>
<td>Relative-extinction</td>
<td>(r)</td>
<td>Uniform (0, 1)</td>
</tr>
</tbody>
</table>

Notes: See the main text for complete description of model parameters and prior distributions. \(\Psi_1\) represents the length of tree \(\Psi\) and \(C_m\) is the maximum chromosome number allowed.

\[
\frac{dE(t)}{dt} = \sum_{j=1}^{C_m} \sum_{k=1}^{C_m} \kappa_{jk} + \sum_{j=1}^{C_m} \epsilon_j E(t) \left(1 - \mu - \frac{\sum_{j=1}^{C_m} \epsilon_j E(t)}{\sum_{j=1}^{C_m} \kappa_{jk} + \sum_{j=1}^{C_m} \epsilon_j E(t) E_l(t)}\right),
\]

(14)
during the forward-time root-to-tip pass to draw ancestral states from their joint distribution conditioned on the model parameters and observed chromosome counts. For more details and validation of our method to estimate ancestral states, please see Supplementary Appendix S1 available on Dryad at http://dx.doi.org/10.5061/dryad.46m4b.

Priors.—Model parameter priors are listed in Table 1. Our implementation allows all priors to be easily modified so that their impact on results can be effectively assessed. Priors for anagenetic rate parameters are given an exponential distribution with a mean of \(2/\Psi_1\) where \(\Psi_1\) is the length of the tree \(\Psi\). This corresponds to a mean rate of two events over the observed tree. The priors for the rate modifiers \(\gamma_m\) and \(b_m\) are assigned a uniform distribution with the range \(-3/C_m\) to \(3/C_m\). This sets minimum and maximum bounds on the amount the rate modifiers can affect the rates of gain and loss at the maximum chromosome number to \(\gamma_m e^{-3} = 0.050\) and \(b_m e^{-3} = 0.050\), respectively.

The speciation rates are drawn from an exponential prior with a mean equal to an estimate of the net diversification rate \(\hat{d}\). Under a constant rate birth–death process not conditioning on survival of the process, the expected number of lineages at time \(t\) is given by:

\[
E(N_t) = N_0 e^{\lambda - \mu t},
\]

(15)
where \(N_0\) is the number of lineages at time 0 and \(d\) is the net diversification rate \(\lambda - \mu\) (Nee et al. 1994; Höhna 2015). Therefore, we estimate \(\hat{d}\) as:

\[
\hat{d} = \frac{(\ln N_t - \ln N_0)/t}{t},
\]

(16)
where \(N_t\) is the number of lineages in the observed tree that survived to the present, \(t\) is the age of the root, and \(N_0 = 2\).

The extinction rate \(\mu\) is given by:

\[
\mu = r \times \lambda = r (\lambda_c + \lambda_t + \lambda_c + \nu_c + \eta_c),
\]

(17)
where \(\lambda_c\) is the total speciation rate and \(r\) is the relative extinction rate. The relative extinction rate \(r\) is assigned a uniform (0,1) prior distribution, thus forcing the extinction rate to be smaller than the total speciation rate. The root frequencies of chromosome numbers \(\pi\) are drawn from a flat Dirichlet distribution.

Model Uncertainty and Selection

Model averaging.—To account for model uncertainty we calculate the posterior density of chromosome evolution model parameters \(\theta\) without conditioning on any single model of chromosome evolution. For each of the 1024 chromosome models \(M_k\), where \(k = 1, 2, \ldots, 1024\), the posterior distribution of \(\theta\) is

\[
P(\theta|D) = \sum_{k=1}^K P(\theta|D, M_k)P(M_k|D).
\]

(18)
Here we average over the posterior distributions conditioned on each model weighted by the model’s posterior probability. We assume an equal prior probability for each model \(P(M_k) = 2^{-10}\).

Reversible jump Markov chain Monte Carlo.—To sample from the space of all possible chromosome evolution models, we employ reversible jump MCMC (Green 1995). This algorithm draws samples from parameter spaces of differing dimensions, and in stationarity samples each model in proportion to its posterior
probability. This permits inference of each model’s fit to the data while simultaneously accounting for model uncertainty.

Our reversible jump MCMC moves between models of different dimensions using augment and reduce moves (Huelsenbeck et al. 2000; Pagel and Meade 2006; May et al. 2016). The reduce move proposes that a parameter should be removed from the current model by setting its value to 0.0, effectively disallowing that class of evolutionary event. Augment moves reverse reduce moves by allowing the parameter to once again have a nonzero value. Both augment and reduce moves operate on all chromosome rate parameters except for \( \phi c \), the rate of no cladogenetic change. Thus the least complex model the MCMC can sample from is one in which \( \phi c > 0.0 \) and all other chromosome rate parameters are set to 0.0, corresponding to a model of no chromosomal changes over the phylogeny. The prior probability of reducing or augmenting model \( M_k \) is \( P(M_k) = P_a(M_k) = 0.5 \).

Bayes factors.—In some cases we wish to compare the fit of models to summarize the mode of evolution within a clade. Bayes factors (Kass and Raftery 1995) compare the evidence between two competing models \( M_i \) and \( M_j \):

\[
B_{ij} = \frac{P(D|M_i)}{P(D|M_j)} \frac{P(M_i)}{P(M_j)}.
\]

(19)

In words, the Bayes factor \( B_{ij} \) is given by the ratio of the posterior odds to the prior odds of the two models. Unlike other methods of model selection such as Akaike Information Criterion (AIC; Akaike 1974) and the Bayesian Information Criterion (BIC; Schwarz 1978), Bayes factors take into account the full posterior densities of the model parameters and do not rely on point estimates. Furthermore AIC and BIC ignore the priors assigned to parameters, whereas Bayes factors penalizes parameters based on the informativeness of the prior. If the prior is informative but overlaps little with the likelihood it is penalized more than a diffuse uninformative prior that allows the parameter to take on whatever value is informed by the data (Nie et al. 2011).

Implementation

The model and MCMC analyses described here are implemented in C++ in the software RevBayes (Höhna et al. 2016). In Supplementary Appendix S1 available on Dryad, we validated our SSE likelihood calculations and ancestral state estimates against those of the R package diversitree (FitzJohn 2012). Rev scripts that specify the chromosome number evolution model (ChromoSSE) described here as a probabilistic graphical model (Höhna et al. 2014) and run the empirical analyses in RevBayes are available at http://github.com/wf8/ChromoSSE. The RevGadgets R package (available at https://github.com/revbayes/RevGadgets) contains functions to summarize results and generate plots of inferred ancestral chromosome numbers over a phylogeny.

The MCMC proposals used are outlined in Supplementary Appendix S2 available on Dryad. Aside from the reversible jump MCMC proposals described above, all other proposals are standard except for the ElementSwapSimplex move operated on the Dirichlet distributed root frequencies parameter. This move randomly selects two elements \( r_1 \) and \( r_2 \) from the root frequencies vector and swaps their values. The reverse move, swapping the original values of \( r_1 \) and \( r_2 \) back, will have the same probability as the initial move since \( r_1 \) and \( r_2 \) were drawn from a uniform distribution. Thus, the Hastings ratio is 1 and the ElementSwapSimplex move is a symmetric Metropolis move.

Simulations

We conducted a series of simulations to: 1) test the effect of unobserved speciation events due to extinction on chromosome number estimates when using a model that does not account for unobserved speciation, 2) compare the accuracy of models of chromosome evolution that account for unobserved speciation versus those that do not, 3) test the effect of jointly estimating speciation and extinction rates with chromosome number evolution, 4) test for identifiability of cladogenetic parameters, and 5) test the effect of incomplete sampling of extant lineages on ancestral chromosome number estimates. We will refer to each of the five simulations above as experiment 1, experiment 2, experiment 3, experiment 4, and experiment 5. Detailed descriptions of each experiment and the methods used to simulate trees and chromosome counts are in Supplementary Appendix S3 available on Dryad.

For all five experiments, MCMC analyses were run for 5000 iterations, where each iteration consisted of 28 different moves in a random move schedule with 79 moves per iteration (see Supplementary Appendix S2 available on Dryad). Samples were drawn with each iteration, and the first 1000 samples were discarded as burn in. Effective sample sizes (ESS) for all parameters in all simulation replicates were over 200, and the mean ESS values of the posterior for the replicates was 1470.3. See Supplementary Appendix S4 available on Dryad for more on convergence of simulation replicates. To perform all five experiments, 2100 independent MCMC analyses were run requiring a total of 89,170.6 CPU h on the Savio computational cluster at the University of California, Berkeley.

Summarizing simulation results.—To summarize the results of our simulations, we measured the accuracy of ancestral state estimates as the percent of simulation replicates in which the true root chromosome number 8 was found to be the maximum a posteriori (MAP) estimate. To evaluate the uncertainty of the simulations, we calculated the mean posterior probability of root
chromosome number for the simulation replicates that correctly found 8 to be the MAP estimate. We also calculated the proportion of simulation replicates for which the true model of chromosome number evolution used to simulate the data (as given by the table in Supplementary Appendix S3 available on Dryad) was estimated to be the MAP model, and calculated the mean posterior probabilities of the true model. To compare the accuracy of model averaged parameter value estimates we calculated coverage probabilities. Coverage probabilities are the percentage of simulation replicates for which the true parameter value falls within the 95% highest posterior density (HPD). High accuracy is shown when coverage probabilities approach 1.0.

Empirical Data

Phylogenetic data and chromosomes counts from five plant genera were analyzed (see Table 2). Like in Mayrose et al. (2010) we assumed each species had a single cytotype, however polymorphism could be accounted for by a vector of probabilities for each chromosome count. Sequence data for Aristolochia was downloaded from TreeBASE (Vos et al. 2010) study ID 1586, Sequences for Helianthus, Mimulus sensu lato, and Primula were downloaded directly from GenBank (Benson et al. 2005), reconstructing the sequence matrices from Timme et al. (2007), Beardsley et al. (2004), and Guggisberg et al. (2009). For each of these four data sets phylogenetic analyses were performed with all gene regions concatenated and unpartitioned, assuming the general time-reversible (GTR) nucleotide substitution model (Tavaré 1986; Rodriguez et al. 1990) with among-site rate variation modeled using a discretized gamma distribution (Yang 1994) with four rate categories. Since divergence time estimation in years is not the objective of this study, and only relative branching times are needed for our models of chromosome number evolution, a birth-death tree prior was used with a fixed root age of 10.0 time units. The MCMC analyses were performed in RevBayes, and were sampled every 100 iterations and run for a total of 400000 iterations, with samples from the first 100000 iterations discarded as burnin. Convergence was assessed by ensuring that the ESS for all parameters was over 200. The maximum a posteriori tree was calculated and used for further chromosome evolution analyses. For Carex section Spirostachyaue the time calibrated tree from Escudero et al. (2010) was used.

Ancestral chromosome numbers and chromosome evolution model parameters were then estimated for each of the five clades. Since testing the effect of incomplete taxon sampling on chromosome evolution inference of the empirical data sets was not a goal of this work, we focus here on results using a taxon sampling fraction \( s \) of 1.0 (though see the Discussion section for more on this). MCMC analyses were run in RevBayes for 11000 iterations, where each iteration consisted of 28 different Metropolis–Hastings moves in a random move schedule with 79 moves per iteration (see Supplementary Appendix S2 available on Dryad). Samples were drawn each iteration, and the first 1000 samples were discarded as burn in. ESS for all parameters were over 200. For all data sets except Primula we used priors as outlined in Table 1. To demonstrate the flexibility of our Bayesian implementation and its capacity to incorporate prior information we used an informative prior for the root chromosome number in the Primula section Aluritia analysis. Our data set for Primula section Aluritia also included samples from Primula sections Armerina and Sikkimensis. Since we were most interested in estimating chromosome evolution within section Aluritia, we used an informative Dirichlet prior \( \{1,1,1,1\} \) (with 100 on the 11th element) to bias the root state towards the reported base number of Primula \( n = 11 \) (Conti et al. 2000). Note all priors can be easily modified in our implementation, thus the impact of priors can be efficiently tested.

Table 2. Empirical data sets analysed

<table>
<thead>
<tr>
<th>Clade</th>
<th>Study</th>
<th>Gene region</th>
<th>Alignment length (bp)</th>
<th>Number of OTUs</th>
<th>Haploid chromosome numbers range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aristolochia</td>
<td>Oba-Toma et al. (2006)</td>
<td>matK</td>
<td>1265</td>
<td>34</td>
<td>3–16</td>
</tr>
<tr>
<td>Helianthus</td>
<td>Timme et al. (2007)</td>
<td>ETS</td>
<td>3085</td>
<td>102</td>
<td>17–51</td>
</tr>
<tr>
<td>Mimulus sensu lato</td>
<td>Beardsley et al. (2004)</td>
<td>trnL, intron, ETS, ITS</td>
<td>2210</td>
<td>115</td>
<td>8–46</td>
</tr>
<tr>
<td>Primula section Aluritia</td>
<td>Guggisberg et al. (2009)</td>
<td>rpl16 intron, rps16 intron, trnL, intron, trnL-trnF spacer, trnT-trnF spacer, trnD-trnT region</td>
<td>5705</td>
<td>56</td>
<td>9–36</td>
</tr>
</tbody>
</table>
TABLE 3. Experiment 1 results: the effect of ignoring unobserved speciation events on chromosome evolution estimates

<table>
<thead>
<tr>
<th>Unobserved speciation events included when simulating data?</th>
<th>Mode of evolution used to simulate data</th>
<th>True root state estimated (%)</th>
<th>Mean posterior of true root state (%)</th>
<th>True model estimated (%)</th>
<th>Mean posterior of true model (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>No</td>
<td>Cladogenetic</td>
<td>93</td>
<td>0.92</td>
<td>13</td>
<td>0.10</td>
</tr>
<tr>
<td>No</td>
<td>Anagenetic</td>
<td>89</td>
<td>0.91</td>
<td>31</td>
<td>0.12</td>
</tr>
<tr>
<td>No</td>
<td>Mixed</td>
<td>88</td>
<td>0.84</td>
<td>0</td>
<td>0.0</td>
</tr>
<tr>
<td>Yes</td>
<td>Cladogenetic</td>
<td>78</td>
<td>0.87</td>
<td>15</td>
<td>0.09</td>
</tr>
<tr>
<td>Yes</td>
<td>Anagenetic</td>
<td>83</td>
<td>0.91</td>
<td>36</td>
<td>0.12</td>
</tr>
<tr>
<td>Yes</td>
<td>Mixed</td>
<td>62</td>
<td>0.80</td>
<td>2</td>
<td>0.10</td>
</tr>
</tbody>
</table>

Notes: Regardless of the true mode of chromosome evolution, the presence of unobserved speciation events in the process that generated the simulated data decreased accuracy in estimating the true root state. The columns from left to right are: 1) an indication of whether or not the data was simulated with a process that included unobserved speciation, 2) the true mode of chromosome evolution used to simulate the data, (for description see main text and Supplementary Appendix S3 available on Dryad), 3) the percent of simulation replicates in which the true chromosome number at the root used to simulate the data was found to be the MAP model, 4) the mean posterior probability of the MAP estimate of the true root chromosome number, 5) the percent of simulation replicates in which the true model used to simulate the data was also found to be the MAP model, and 6) the mean posterior probability of the MAP estimate of the true model.

RESULTS

Simulations

General results.—In all simulations, the true model of chromosome number evolution was infrequently estimated to be the MAP model (<36% of replicates), and when it was the posterior probability of the MAP model was very low (<0.12, Table 3). We found that the accuracy of root chromosome number estimation was similar whether the process that generated the simulated data was cladogenetic-only or anagenetic-only (Tables 3 and 4). However, when the data was simulated under a process that included both cladogenetic and anagenetic evolution we found a decrease in accuracy in the root chromosome number estimates in all cases.

Experiment 1 results.—The presence of unobserved speciation in the process that generated the simulated data decreased the accuracy of ancestral state estimates (Fig. 3, Table 3). Similarly, uncertainty in root chromosome number estimates increased with unobserved speciation (lower mean posterior probabilities; Table 3). The accuracy of parameter value estimates as measured by coverage probabilities was similar (results not shown).

Experiment 2 results.—When comparing estimates from ChromoSSE that account for unobserved speciation to estimates from the non-SSE model that does not account for unobserved speciation, we found that the accuracy in estimating model parameter values was mostly similar, though for some cladogenetic parameters there was higher accuracy with the model that did account for unobserved speciation (ChromoSSE; Fig. 4). For both models estimates of cladogenetic parameters were more accurate than estimates of anagenetic parameters when the true generating model included cladogenetic changes.

We found that ChromoSSE had more uncertainty in root chromosome number estimates (lower mean posterior probabilities) compared with the non-SSE model that did not account for unobserved speciation. Similarly, the root chromosome number was estimated with slightly lower accuracy (Table 4).

Experiment 3 results.—We found that jointly estimating speciation and extinction rates with chromosome number evolution using ChromoSSE slightly decreased the accuracy of root chromosome number estimates, and further it increased the uncertainty of the inferred root chromosome number (as reflected in lower mean posterior probabilities; Table 4).Fixing the speciation and extinction rates to their true value removed much of the increased uncertainty associated with using a model that accounts for unobserved speciation (Table 4).

Experiment 4 results.—Under simulation scenarios that had cladogenetic changes but no anagenetic changes, we found that ChromoSSE overestimated anagenetic parameters and underestimated cladogenetic parameters (Fig. 5a), which explains the lower coverage probabilities of cladogenetic parameters reported above for experiment 2 (Fig. 4). When anagenetic parameters were fixed to 0.0 cladogenetic parameters were no longer underestimated (Fig. 5a), and the coverage probabilities of cladogenetic parameters increased slightly (Fig. 5b).

Experiment 5 results.—We found that incomplete sampling of extant lineages had a minor effect on the accuracy of ancestral chromosome number estimates (Fig. 6). Accuracy only slightly decreased as the percentage of extant lineages sampled declined from 100% to 50%, and decreased more rapidly when the percentage went to 10%. As measured by the proportion of simulation replicates that inferred the MAP root...
chromosome number to be the true root chromosome number, the accuracy of ancestral states estimated under ChromoSSE declined from 0.80 accuracy at 100% taxon sampling to 0.69 at 10% taxon sampling. Essentially no difference in accuracy was detected between the non-SSE model that does not take unobserved speciation into account and ChromoSSE. Furthermore, little difference in accuracy was detected using ChromoSSE with the taxon sampling probability \( p_s \) set to 1.0 compared with ChromoSSE with \( p_s \) set to the true value (0.1, 0.5, or 1.0; Fig. 6).

**Empirical Data**

Model averaged MAP estimates of ancestral chromosome numbers for each of the five empirical data sets are shown in Figures 7–11. The mean model-averaged chromosome number evolution parameter value estimates for the empirical data sets are reported in Table 5. Posterior probabilities for the MAP model of chromosome number evolution were low for all data sets, varying between 0.04 for *Carex* section *Spirostachyae* and 0.21 for *Helianthus* (Table 6). Bayes factors supported
TABLE 4. Experiments 2 and 3 results: the effects of using a model that accounts for unobserved speciation and of jointly estimating diversification rates on ancestral chromosome number estimates

<table>
<thead>
<tr>
<th>Experiment #</th>
<th>Estimates made w/ model that accounted for unobserved speciation?</th>
<th>Specification and extinction rates jointly estimated?</th>
<th>Mode of evolution used to simulate data</th>
<th>True root state estimated (%)</th>
<th>Mean posterior of true root state</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>No</td>
<td>No</td>
<td>Cladogenetic</td>
<td>78</td>
<td>0.87</td>
</tr>
<tr>
<td>2</td>
<td>No</td>
<td>No</td>
<td>Anagenetic</td>
<td>83</td>
<td>0.91</td>
</tr>
<tr>
<td>2</td>
<td>No</td>
<td>No</td>
<td>Mixed</td>
<td>62</td>
<td>0.80</td>
</tr>
<tr>
<td>2 and 3</td>
<td>Yes</td>
<td>Yes</td>
<td>Cladogenetic</td>
<td>78</td>
<td>0.81</td>
</tr>
<tr>
<td>2 and 3</td>
<td>Yes</td>
<td>Yes</td>
<td>Anagenetic</td>
<td>80</td>
<td>0.86</td>
</tr>
<tr>
<td>2 and 3</td>
<td>Yes</td>
<td>Yes</td>
<td>Mixed</td>
<td>61</td>
<td>0.72</td>
</tr>
<tr>
<td>3</td>
<td>Yes</td>
<td>No</td>
<td>Cladogenetic</td>
<td>78</td>
<td>0.84</td>
</tr>
<tr>
<td>3</td>
<td>Yes</td>
<td>No</td>
<td>Anagenetic</td>
<td>83</td>
<td>0.90</td>
</tr>
<tr>
<td>3</td>
<td>Yes</td>
<td>No</td>
<td>Mixed</td>
<td>62</td>
<td>0.76</td>
</tr>
</tbody>
</table>

Note: This table compares estimates of chromosome evolution using a non-SSE model that does not account for unobserved speciation events with ChromoSSE that does account for unobserved speciation events (Experiment 2), and compares estimates of chromosome evolution when jointly estimated with speciation and extinction rates versus when the true speciation and extinction rates are given (Experiment 3). Regardless of the true mode of chromosome evolution, the use of a model that accounts for unobserved speciation increases uncertainty in root state estimates. The columns from left to right are: 1) an indication of which experiment the results pertain to, 2) an indication of whether or not the estimates were made with ChromoSSE (that accounts for unobserved speciation), 3) whether diversification rates were jointly estimated with chromosome evolution, 4) the percent of simulation replicates in which the true chromosome number at the root used to simulate the data was found to be the MAP estimate, 5) the mean posterior probability of the MAP estimate of the true root chromosome number.

FIGURE 5. Experiment 4 results: testing identifiability of cladogenetic parameters under ChromoSSE. a) Chromosome parameter value estimates from 100 simulation replicates under a simulation scenario with no anagenetic changes (cladogenetic only). The stars represent true values. The box plots compare parameter estimates made when anagenetic parameters were fixed to 0 to estimates made when all parameters were free. When all parameters were free the anagenetic parameters were overestimated and cladogenetic parameters were underestimated. When the anagenetic parameters were fixed to 0 the estimates for the cladogenetic parameters were more accurate. b) Coverage probabilities of chromosome evolution parameters under the cladogenetic only model of chromosome evolution. The accuracy of cladogenetic parameter estimates increased when anagenetic parameters were fixed to 0.

unique, clade-specific combinations of anagenetic and cladogenetic parameters for all five data sets (Table 6). None of the clades had support for purely anagenetic or purely cladogenetic models of chromosome evolution.

The ancestral state reconstructions for Aristolochia were highly similar to those found by Mayrose et al. (2010). We found a moderately supported root chromosome number of 8 (posterior probability 0.45), and a polyploidization event on the branch leading to the Isotrema clade which has a base chromosome number of 16 with high posterior probability (0.88; Fig. 7). On the branch leading to the main Aristolochia clade we found a dysploid loss of a single chromosome. Overall, we estimated moderate rates of anagenetic
dysploid and polyploid changes, and the rates of cladogenetic change were 0 except for a moderate rate of cladogenetic dysploid loss (Tables 5). There was only one cladogenetic change inferred in the MAP ancestral state reconstruction, which was a recent possible dysploid speciation event that split the sympatric west-central Mexican species *Aristolochia tentaculata* and *A. taliscana*.

In *Helianthus*, on the other hand, we found high rates of cladogenetic polyploidization, and low rates of anagenetic change (Tables 5). Twelve separate possible polyploid speciation events were identified over the phylogeny (Fig. 8), and cladogenetic polyploidization made up 16% of all observed and unobserved speciation events. Bayes factors gave very strong support for models that included cladogenetic polyploidization as well as anagenetic demi-polyploidization (Table 6), the latter explaining the frequent anagenetic transitions from 34 to 51 chromosomes found in the MAP ancestral state reconstruction. The well supported root chromosome number of 17 (posterior probability 0.91) corresponded with the findings of Mayrose et al. (2010).

As opposed to the *Helianthus* results, the *Carex* section *Spirostachyae* estimates had very low rates of polyploidization and instead had high rates of cladogenetic dysploid change (Table 5). An estimated 36.9% of all observed and unobserved speciation events included a cladogenetic gain or loss of a single chromosome. Overall, the rates of anagenetic changes were estimated to be much lower than the rates of cladogenetic changes. Bayes factors did not support either anagenetic or cladogenetic polyploidization (Table 6). The MAP root chromosome number of 37, despite being very weakly supported (0.08), corresponds with the findings of Escudero et al. (2014), where it was also poorly supported (Fig. 9).

In *Primula*, we found a base chromosome number for section *Aleuritia* of 9 with high posterior probability (0.82; Fig. 10), which agrees with estimates from Glick and Mayrose (2014). We estimated moderate rates of anagenetic and cladogenetic changes, including both cladogenetic polyploidization and demi-polyploidization (Table 5). The MAP ancestral state estimates include an inferred history of possible polyploid and demi-polyploid speciation events in the clade containing the tetraploid *Primula halleri* and the hexaploid *P. scotica*. *Primula* is the only data set out of the five analysed here for which Bayes factors supported the inclusion of cladogenetic demi-polyploidization (Table 6).
FIGURE 7. Ancestral chromosome number estimates of Aristolochia. The model averaged MAP estimate of ancestral chromosome numbers are shown at each branch node. The states of each daughter lineage immediately after cladogenesis are shown at the "shoulders" of each node. The size of each circle is proportional to the chromosome number and the color represents the posterior probability. The MAP root chromosome number is 8 with a posterior probability of 0.45. The grey arrow highlights the possible dysploid speciation event leading to the west-central Mexican species Aristolochia tentaculata and A. taliscana. Clades corresponding to subgenera are indicated at right.

The well supported root chromosome number of 8 (posterior probability 0.90) found for Mimulus s.l. corresponds with the inferences reported in Beardsley et al. (2004). We estimated moderate rates of anagenetic dysploid gains and losses, as well as a moderate rate of cladogenetic polyploidization (Table 5). Bayes factors also supported models that included anagenetic dysploid gain and loss, as well as cladogenetic polyploidization (Table 6). The MAP ancestral state reconstruction revealed that most of the possible polyploid speciation events took place in the Diplacus clade, particularly in the clade containing the tetraploids Mimulus cupreus, M. glabratus, M. luteus, and M. yecorensis (Fig. 11). Additionally, an ancient cladogenetic polyploidization event is inferred for the split between the two main Diplacus clades at about 5 million time units ago.

DISCUSSION

The results from the empirical analyses show that the ChromoSSE models detect strikingly different modes of chromosome evolution with clade-specific combinations of anagenetic and cladogenetic processes. Anagenetic dysploid changes were supported in nearly all clades; however, cladogenetic dysploid changes were only supported in Carex. The occurrence of anagenetic dysploid changes in all clades suggest that small chromosome number changes due to gains and losses
may frequently have a minimal effect on the formation of reproductive isolation, though our results suggest that *Carex* may be a notable exception. Anagenetic polyploidization was only supported in *Aristolochia*, while cladogenetic polyploidization was supported in *Helianthus*, *Mimusus* s.l., and *Primula*. These findings confirm the evidence presented by *Zhan et al.* (2016) that polyploidization events could play a significant role during plant speciation.

Our models shed new light on the importance of whole genome duplications as a key driver in evolutionary diversification processes. *Helianthus* has long been understood to have a complex history of polyploid speciation (*Timme et al.* 2007), but our results here are the first to statistically show the prevalence of cladogenetic polyploidization in *Helianthus* (occurring at 16% of all speciation events) and how few of the chromosome changes are estimated to be anagenetic. Polyploid speciation has also been suspected to be common in *Mimusus* s.l. (*Vickery* 1995), and indeed we estimated that 7% of speciation events were cladogenetic polyploidization events. We also estimated that the rates of cladogenetic dysploidization in *Mimusus* s.l. were 0, which is in contrast to the parsimony based inferences presented in *Beardsley et al.* (2004), which estimated 11.5% of all speciation events included polyploidization and 13.3% included dysploidization. Their estimates, however, did not distinguish cladogenetic from anagenetic processes, and so they likely underestimated anagenetic changes. Our ancestral state reconstructions of chromosome number evolution for *Helianthus*, *Mimusus* s.l., and *Primula* show that polyploidization events generally occurred in the relatively recent past; few ancient polyploidization events were reconstructed...
Figure 9. Ancestral chromosome number estimates of Carex section Spirostachyae. The model averaged MAP estimate of ancestral chromosome numbers are shown at each branch node. The states of each daughter lineage immediately after cladogenesis are shown at the "shoulders" of each node. The size of each circle is proportional to the chromosome number and the color represents the posterior probability. The MAP root chromosome number is 37 with a posterior probability of 0.08. Grey arrows indicate the location of possible dysploid speciation events. 36.9% of all speciation events include a cladogenetic gain or loss of a single chromosome. Clades corresponding to subsections are indicated at right. (one exception being the ancient cladogenetic polyploidization event in Mimulus clade Diplacus). This pattern appears to be consistent with recent studies that show polyploid lineages may undergo decreased net diversification (Mayrose et al., 2011; Scarpino et al. 2014), leading some to suggest that polyploidization may be an evolutionary dead-end (Arrigo and Barker 2012). While in the analyses presented here we fixed rates of speciation and extinction through time and across lineages, an obvious extension of our models would be to allow these rates to vary across the tree and statistically test for rate changes in polyploid lineages.

Our findings also suggest dysploid changes may play a significant role in the speciation process of some lineages. The genus Carex is distinguished by holocentric chromosomes that undergo common fusion and fission events but rarely polyploidization (Hipp 2007). This concurs with our findings from Carex section Spirostachyae, where we saw no support for models including either anagenetic or cladogenetic polyploidization. Instead we found high rates of cladogenetic dysploid change, which is congruent with earlier results that show Carex diversification is driven by processes of fission and fusion occurring with cladogenetic shifts in chromosome number (Hipp 2007; Hipp et al. 2007). Hipp (2007) proposed a speciation scenario for Carex in which the gradual accumulation of chromosome fusions, fissions, and rearrangements in recently diverged populations increasingly reduce the fertility of hybrids between populations, resulting in high species richness. More recently, Escudero et al. (2016) found that chromosome number differences...
in *Carex scoparia* led to reduced germination rates, suggesting hybrid dysfunction could spur chromosome speciation in *Carex*. Holocentricity has arisen at least 13 times independently in plants and animals (Melters et al. 2012), thus future work could examine chromosome number evolution in other holocentric clades and test for similar patterns of cladogenetic fission and fusion events.

The models presented here could also be used to further study the role of divergence in genomic architecture during sympatric speciation. Chromosome structural differences have been proposed to perform a central role in sympatric speciation, both in plants (Gottlieb 1973) and animals (Feder et al. 2005; Michel et al. 2010). In *Aristolochia* we found most changes in chromosome number were estimated to be anagenetic, with the only cladogenetic change occurring among a pair of recently diverged sympatric species. By coupling our chromosome evolution models with models of geographic range evolution it would be possible to statistically test whether the frequency of cladogenetic chromosome changes increase in sympatric speciation events compared with allopatric speciation events, thereby testing for interaction between these two different processes of reproductive isolation and evolutionary divergence.

The simulation results from Experiment 1 demonstrate that extinction reduces the accuracy of inferences made by models of chromosome evolution that do not take into account unobserved speciation events. The model averaged MAP estimate of ancestral chromosome numbers are shown at each branch node. The states of each daughter lineage immediately after cladogenesis are shown at the “shoulders” of each node. The size of each circle is proportional to the chromosome number and the color represents the posterior probability. The MAP root chromosome number of section *Aleuritia* is 9 with a posterior probability of 0.82. The arrows show the inferred history of possible polyploid and demi-polyploid speciation events in the clade containing the tetraploids *Primula egaliksensis* and *P. halleri* and the hexaploid *P. scotica*. Clades corresponding to sections are indicated at right.
FIGURE 11. Ancestral chromosome number estimates of Mimulus sensu lato. The model averaged MAP estimate of ancestral chromosome numbers are shown at each branch node. The states of each daughter lineage immediately after cladogenesis are shown at the “shoulders” of each node. The size of each circle is proportional to the chromosome number and the color represents the posterior probability. The MAP root chromosome number is 8 with a posterior probability of 0.90. The arrows highlight the inferred history of repeated polyploid speciation events in the Diplacus clade, which contains the tetraploids Mimulus cupreus, M. glabratus, M. luteus, and M. yecorensis. Clades corresponding to segregate genera are indicated at right.

events. Furthermore, the simulations performed in Experiments 2 and 3 show that the substantial uncertainty introduced in our analyses by jointly estimating diversification rates and chromosome evolution resulted in lower posterior probabilities for ancestral state reconstructions. We feel that this is a strength of our method; the lower posterior probabilities incorporate true uncertainty due to extinction and so represent more conservative estimates. Additionally, the simulation results from Experiment 4 reveal that rates of anagenetic evolution were overestimated and rates of cladogenetic change were underestimated when the generating process consisted only of cladogenetic events. This suggests the possibility that our models of chromosome number evolution are only partially identifiable, and that the results of our empirical analyses may have a similar bias towards overestimating anagenetic evolution and underestimating cladogenetic evolution. This bias may be an issue for all ClaSSE type models, but the practical consequences here are conservative estimates of cladogenetic chromosome evolution.

An important caveat for all phylogenetic methods is that estimates of model parameters and ancestral states can be highly sensitive to taxon sampling (Heath et al. 2008). All of the empirical data sets examined here included nonmonophyletic taxa that were treated as separate lineages. We made the unrealistic assumptions...
that 1) each of the nonhomophyletic lineages sharing a
taxon name have the same cytotype, and 2) the taxon
sampling probability (\(\mu\)) for the birth-death process
was 1.0. The former assumption could drastically affect
ancestral state estimates, but its effect can only be
confirmed by obtaining chromosome counts for each
lineage regardless of taxon name. While the results
from simulation Experiment 5 showed that fixing \(\mu\) to 1.0 did
not decrease the accuracy of inferred ancestral states,
we still performed extra analyses of the empirical data
sets with different values of \(\mu\) (results not shown).
The results indicated that total speciation and extinction
rates are sensitive to \(\mu\), but the relative speciation
rates (e.g. between \(\theta_q\) and \(\gamma_q\)) remained similar. The
ancestral state estimates of cladogenetic and anagenetic
chromosome changes were robust to different values of
\(\mu\). This could vary among data sets and care
should be taken when considering which lineages
to sample.

Bayesian model averaging is particularly appropriate
for models of chromosome number evolution since
conditioning on a single model ignores the considerable
degree of model uncertainty found in
both the simulations and the empirical analyses. In the
simulations the true model of chromosome evolution
was rarely inferred to be the MAP model (<39% of
replicates), and in the instances it was correctly identified
the posterior probability of the MAP model was <0.13.
The posterior probabilities of the MAP models for the
empirical data sets were similarly low, varying between
0.04 and 0.22. Conditioning on a single poorly fitting
model of chromosome evolution, even when it is the
best model available, results in an underestimate of
the uncertainty of ancestral chromosome numbers.
Furthermore, Bayesian model averaging enabled us
to detect different modes of chromosome number
evolution without the limitation of traditional model
testing procedures in which multiple analyses are
performed that each condition on a different single
model. This is a particularly useful approach when the
space of all possible models is large.

Our RevBayes implementation facilitates model
modularity and easy experimentation. Experimenting
with different priors or MCMC moves is achieved by
simply editing the Rev scripts that describe the model.
Though in our analyses here we ignored phylogenetic
uncertainty by assuming a fixed known tree, we could
easily incorporate this uncertainty by modifying a
couple lines of the Rev script to integrate over a
previously estimated posterior distribution of trees. We
could also use molecular sequence data simultaneously
with the chromosome models to jointly infer phylogeny
and chromosome evolution, allowing the chromosome
data to help inform tree topology and divergence times.
In this paper we chose not to perform joint inference so
that we could isolate the behavior of the chromosome
evolution models; however, this is a promising direction
for future research.

There are a number of challenging directions for
future work on phylogenetic chromosome evolution
models. Models that incorporate multiple aspects of
chromosome morphology such as translocations,
 inversions, and other gene synteny data as well as the
presence of ring and/or B chromosomes have yet to

be developed. None of our models currently account for allopolyploidization; indeed few phylogenetic comparative methods can handle reticulate evolutionary scenarios that result from allopolyploidization and other forms of hybridization (Marcussen et al. 2015).

A more tractable problem is mapping chromosome number changes along the branches of the phylogeny, as opposed to simply making estimates at the nodes as we have done here. Since the approach described here models both anagenetic and cladogenetic chromosome evolution processes while accounting for unobserved speciation events, the rejection sampling procedure used in standard stochastic character mapping (Nielsen 2002; Huelserbau et al. 2003) is not sufficient. While data augmentation approaches such as those described by Bokma (2008) could be utilized, they require complex MCMC algorithms that may have difficulty mixing. Another option is to extend the method described in this paper to draw joint ancestral states by numerically integrating root-to-tip over the tree into a new procedure called joint conditional character mapping. This sort of approach would infer the joint MAP history of chromosome changes both at the nodes and along the branches of the tree, and provide an alternative to stochastic character mapping that will work for all ClaSSE type models.

Conclusions

The analyses presented here show that the ChromoSSE models of chromosome number evolution successfully infer different clade-specific modes of chromosome evolution as well as the history of anagenetic and cladogenetic chromosome number changes for a clade, including reconstructing the timing and location of possible chromosome speciation events over the phylogeny. These models will help investigators study the mode and history of chromosome evolution within individual clades of interest as well as advance understanding of how fundamental changes in the architecture of the genome such as whole genome duplications affect macroevolutionary patterns and processes across the tree of life.

SUPPLEMENTARY MATERIAL

Data available from the Dryad Digital Repository: http://dx.doi.org/10.5061/dryad.4en4b.

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